

# Pion data and transport model calculations --Pre-S $\pi$ RIT project

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**Based on the Work for long-waiting Mr. Sako-kun's PhD thesis**

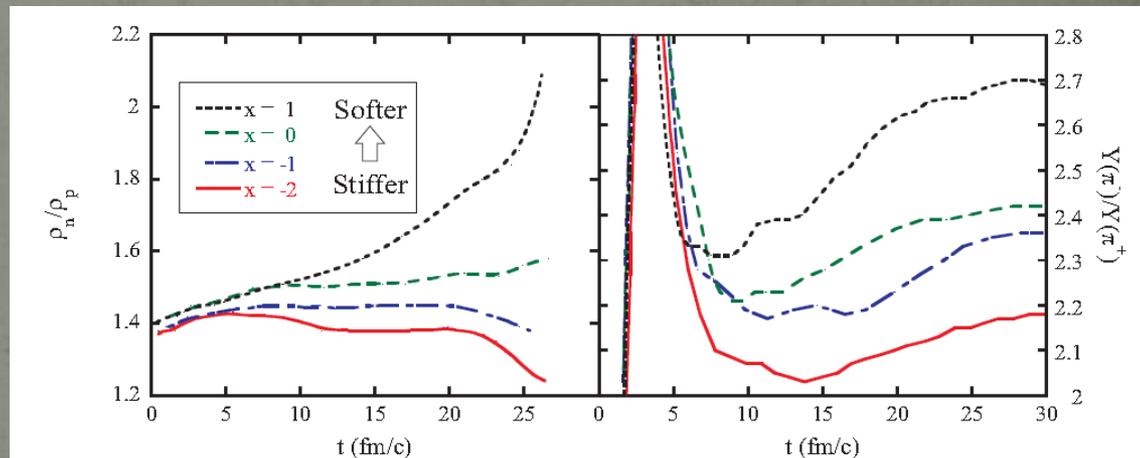
As a probe of symmetry energy  
at high density we made a bet on pions



The **symmetry pressure** at high density would **expel** neutrons and **attract** protons.

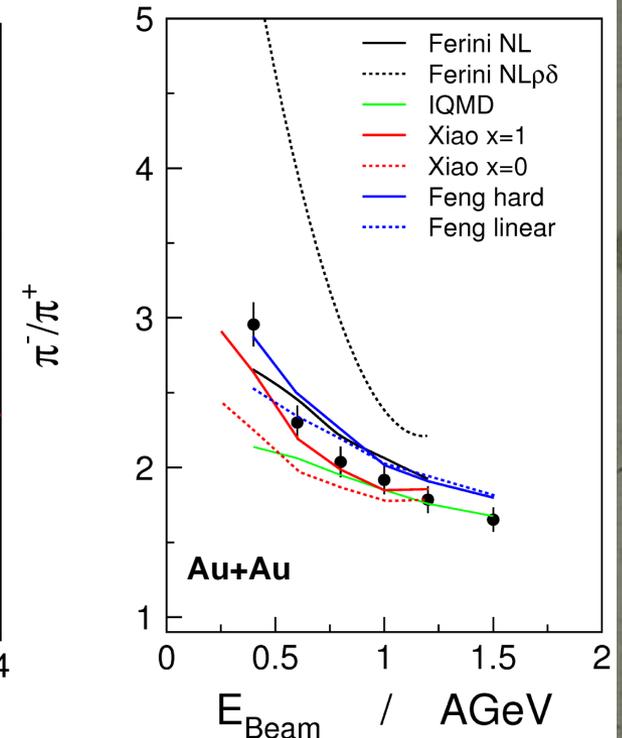
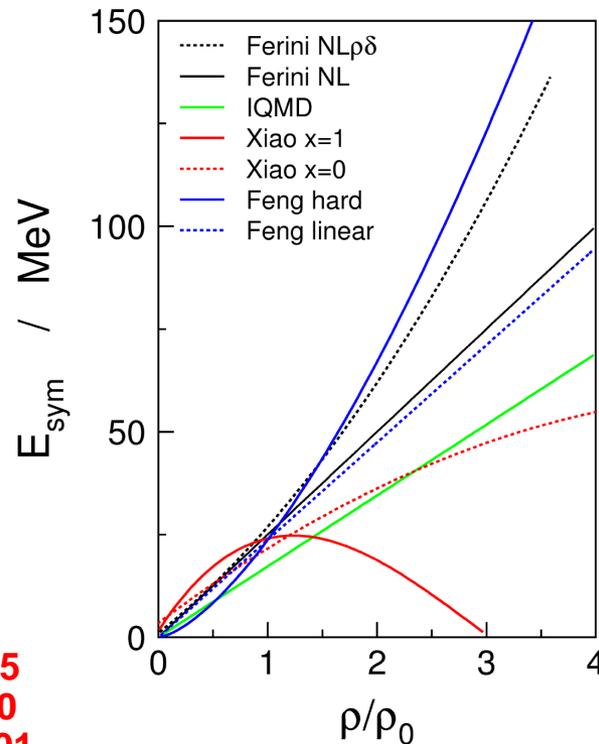
Prediction of  
transport theory

Suppress  $Y(n)/Y(p)$ ,  
 $Y(\pi^-)/Y(\pi^+)$ , etc.



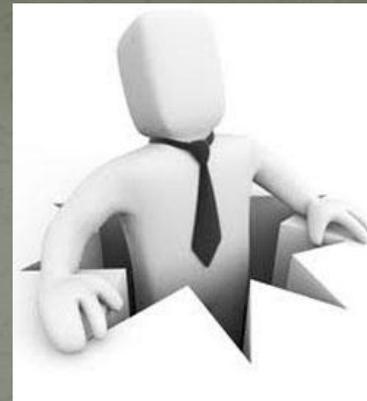
Bao-An Li et al., Phys. Rev. C 71, 014608 (2005)

# Now odds become unclear because of doubt on theoretical prediction

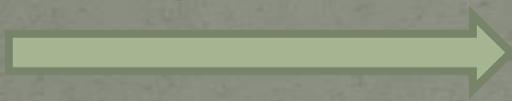


**Z. Xiao et al., PRL 102 (2009) 625**  
**J. Xie et al., PLB 718 (2013) 1510**  
**J. Xu et al., PRC 87 (2013) 067601**  
**G. Ferini et al., PRL 97 (2006) 202301**  
**Z.Q.Feng and G.-M. Jin, PLB 683 (2010) 140**  
**J.Hong, P. Danielewicz, PRC 90 (2014) 024605**

# To make a breakthrough



Should know pion production in heavy-ion collision more clearly.



How well can we account on pion observables?

# Pioneering work by Nagamiya et al.

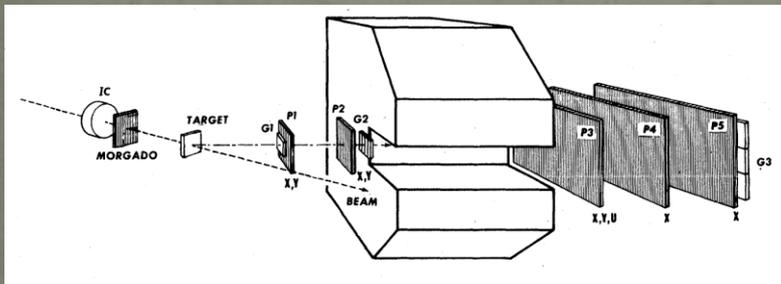
PHYSICAL REVIEW C

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## Production of pions and light fragments at large angles in high-energy nuclear collisions

S. Nagamiya, M.-C. Lemaire,\* E. Moeller,† S. Schnetzer, G. Shapiro, H. Steiner, and I. Tanihata‡  
Lawrence Berkeley Laboratory and Department of Physics, University of California, Berkeley, California 94720  
(Received 9 March 1981)

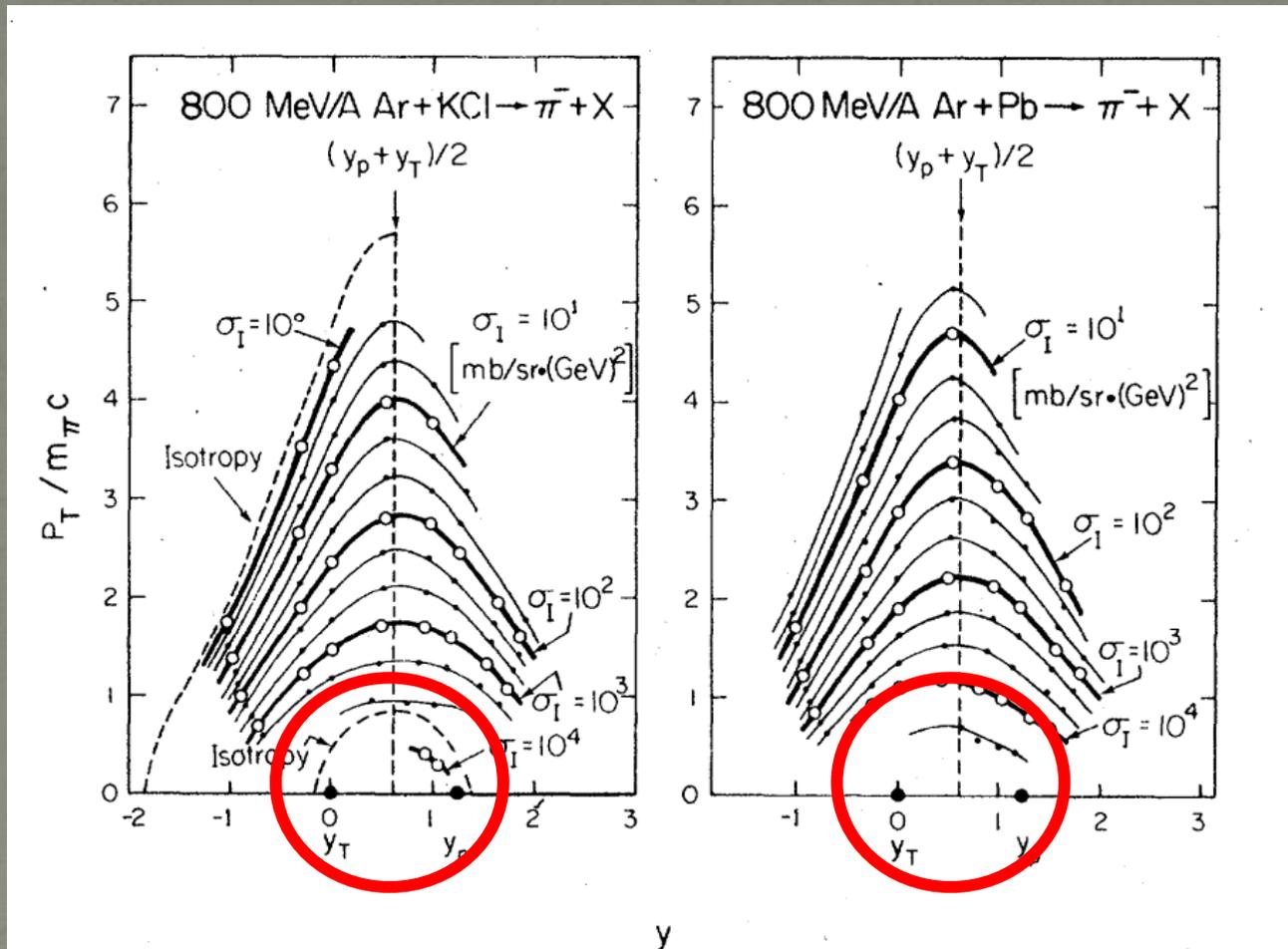


$E_{\text{beam}}^{\text{lab}}/\text{nucl}$ (MeV)	Projectile	Target	Detected particles	Data type available		
				Inclusive	TPC <sup>a</sup>	HME <sup>b</sup>
400	Ne	NaF, Cu, Pb	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}$	Yes	Yes	*
800	C	C, Pb	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}$	Yes	Yes	*
		NaF, Cu, Pb	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}$	Yes	Yes	Yes
2100	Ne	KCl, Pb	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}, {}^4\text{He}$	Yes	Yes	Yes
		NaF, Pb	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}, {}^4\text{He}$	Yes	Yes	Yes
800	$p$	C, NaF, KCl	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}$	Yes	Yes	No
		Cu, Pb				
2100	$p$	C, NaF, KCl	$\pi^{\pm}, p, d, {}^3\text{H}, {}^3\text{He}$	Yes	Yes	No
		Cu, Pb				

<sup>a</sup>TPC—two-particle correlations.

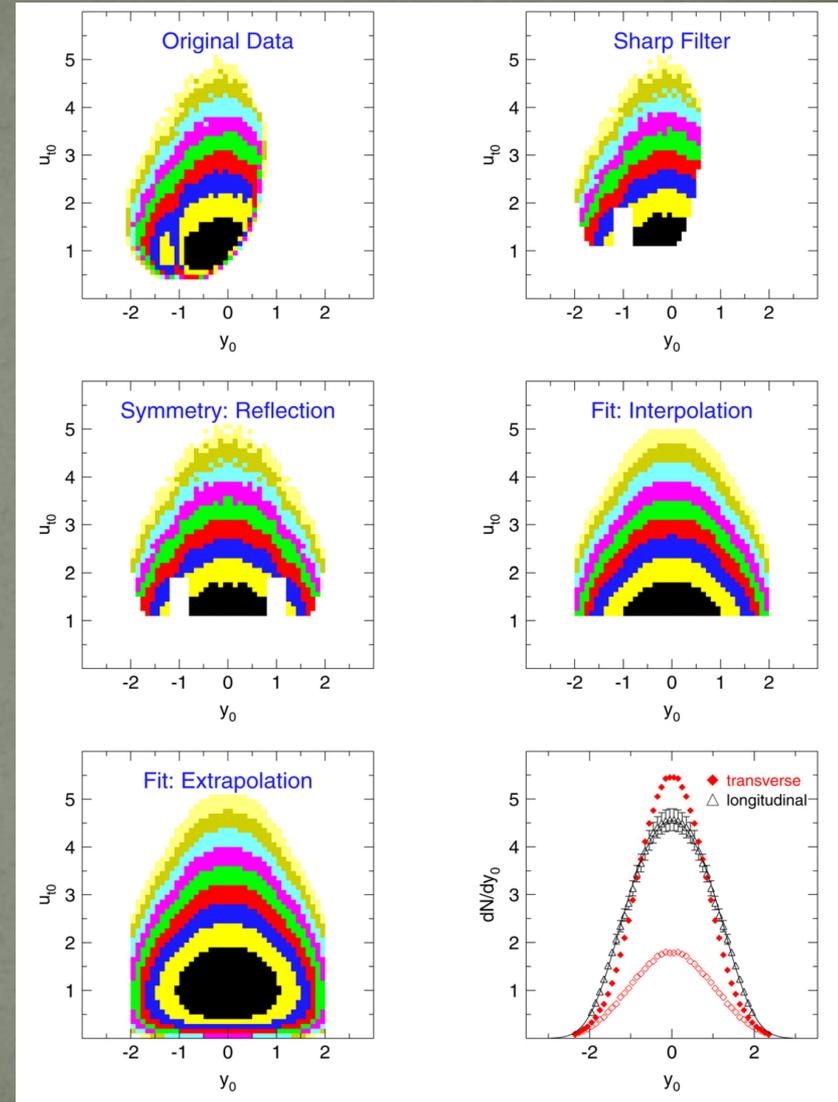
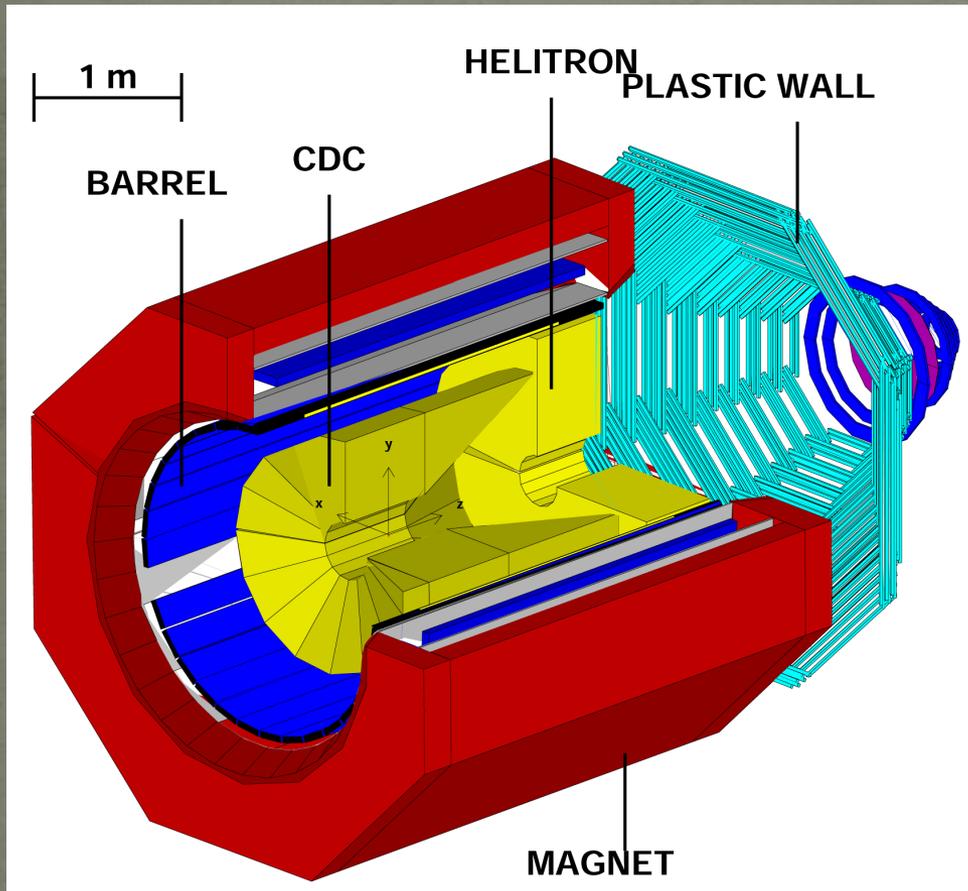
<sup>b</sup>HME—high-multiplicity events.

# Need to integrate differential cross section



Established N-N Cascade type picture

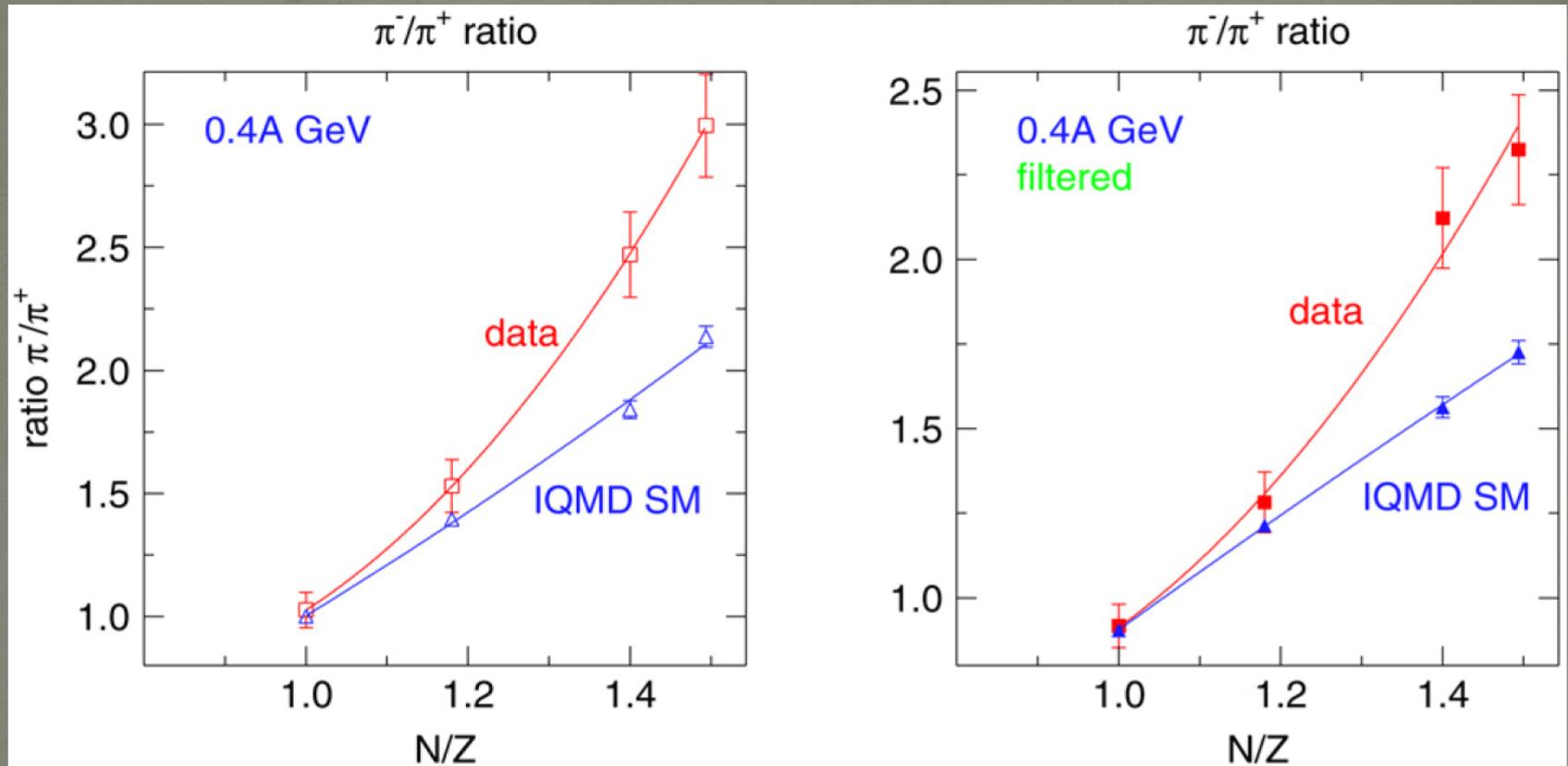
# FOPI @ GSI



reaction (used)	target thickness	isotopic enrich- ment	energy [AMeV]
$^{96}\text{Ru} + ^{96}\text{Ru}$	431 mg/cm <sup>2</sup>	96.52 %	400, 1000, 1528
$^{96}\text{Zr} + ^{96}\text{Zr}$	380 mg/cm <sup>2</sup>	95.6 %	400, 1000, 1528
$^{197}\text{Au} + ^{197}\text{Au}$	202 mg/cm <sup>2</sup>	100 %	400, 1000, 1490
$^{40}\text{Ca} + ^{40}\text{Ca}$	386 mg/cm <sup>2</sup>	96 %	400, 1000, 1500

**Need efficiency correction**

# After all FOPI found.....



# Most of previous experimental studies

- Using mass-symmetric collisions so far

$$(N/Z)_{\text{participant}} \approx (N/Z)_{\text{proj}} \approx (N/Z)_{\text{targ}}$$



- **Over-simplified** the situation

Impossible to distinguish different moving source frames, **like**

**NN cm, participant cm, nucleus-nucleus cm etc.**

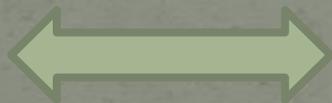


Better study mass-asymmetric collisions

# Well before start data taking of S $\pi$ RIT

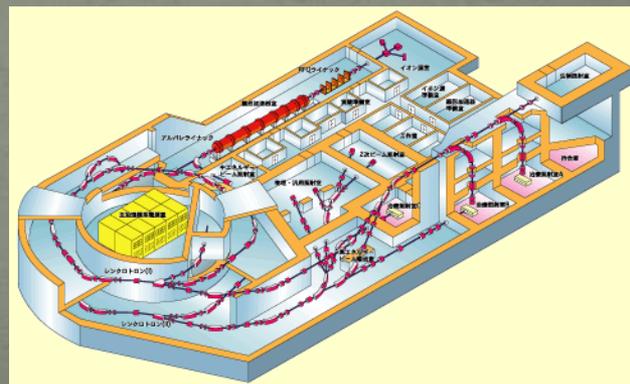
- We started pion experiments using HIMAC since 2007.

RI-beam >> require large acceptance



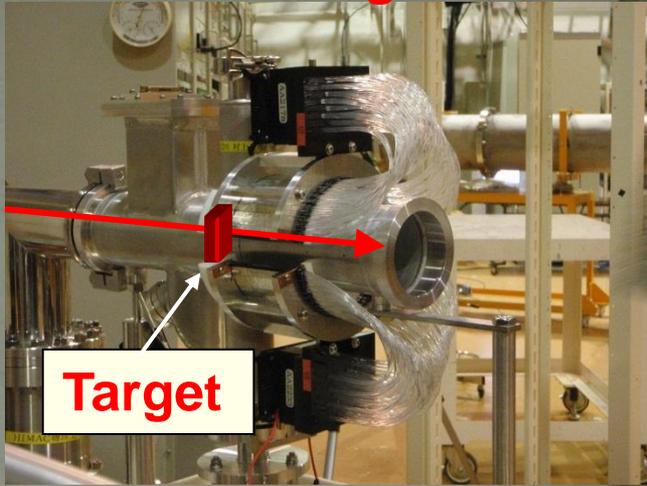
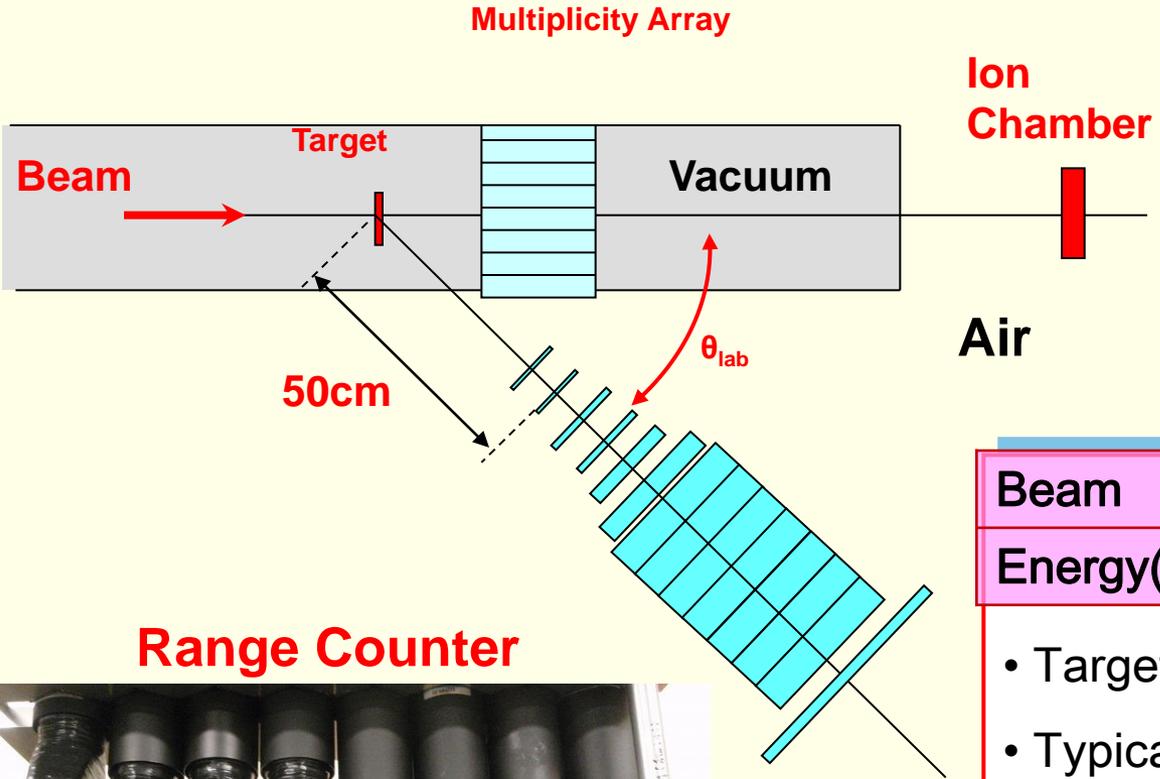
Usual beam >> small acceptance may be usable

HIMAC; Heavy Ion **Medical** Accelerator in Chiba



# Pilot Experiments at HIMAC

Multiplicity Array  
27-58 deg.

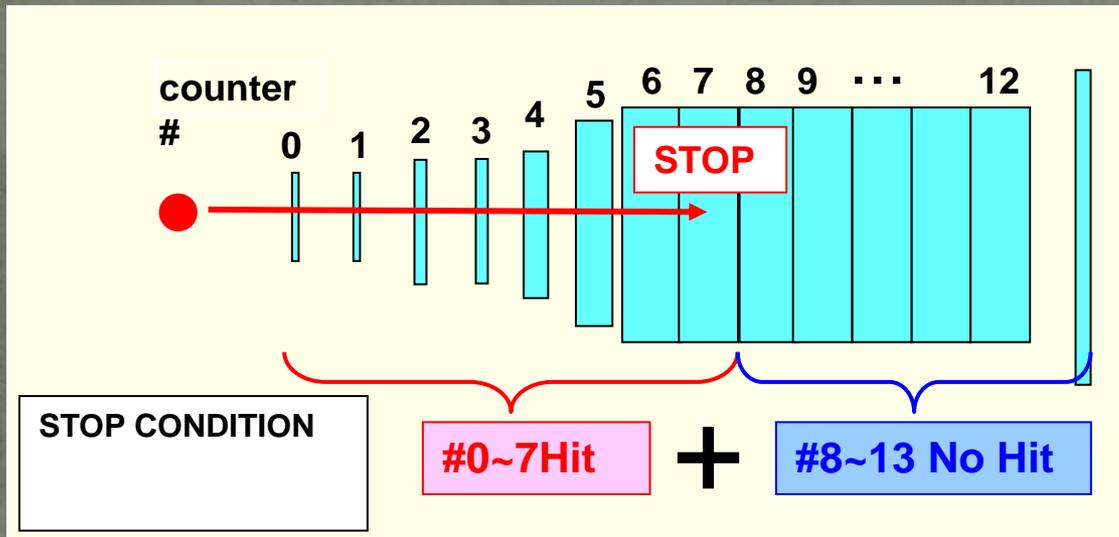


Beam	<b><math>^{28}\text{Si}</math></b>	$^{132}\text{Xe}$
Energy(AMeV)	<b>400, 600, 800</b>	400

- Target : In  $\sim 390 \text{ mg/cm}^2$
- Typical Intensity :  $\sim 10^7$  ppp
- Range Counter : 14 layers (+2) of Sci.
- measured angle ( $\theta_{lab}$ ) : 30, 45, 60, 75, 90, 120 degree
- solid angle : **10 msr**



# Detection Principle



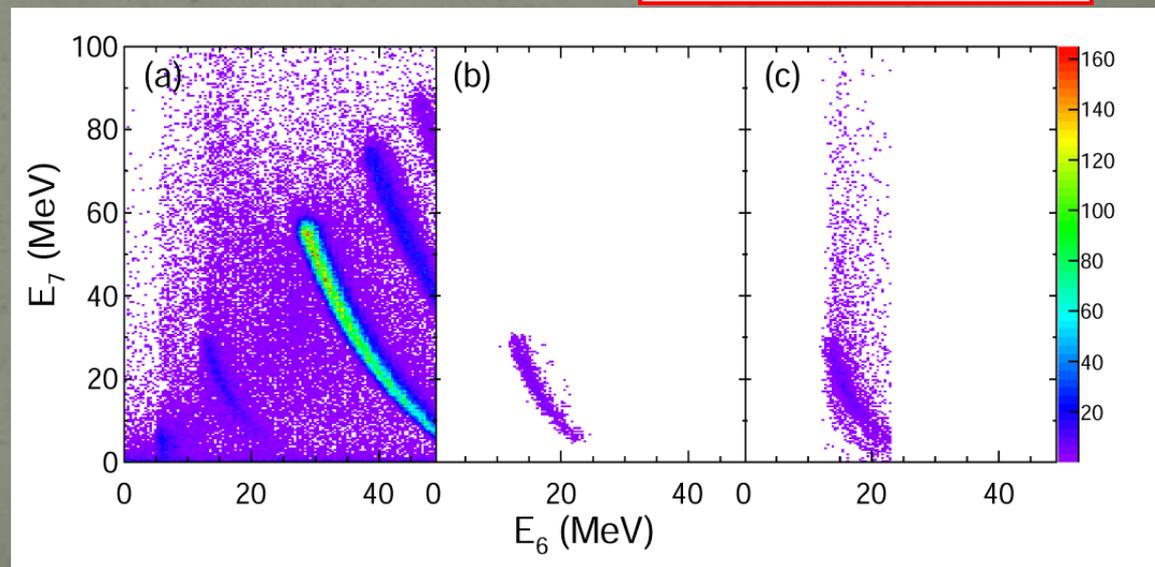
·  $\pi^+$  decay to  $\mu^+$

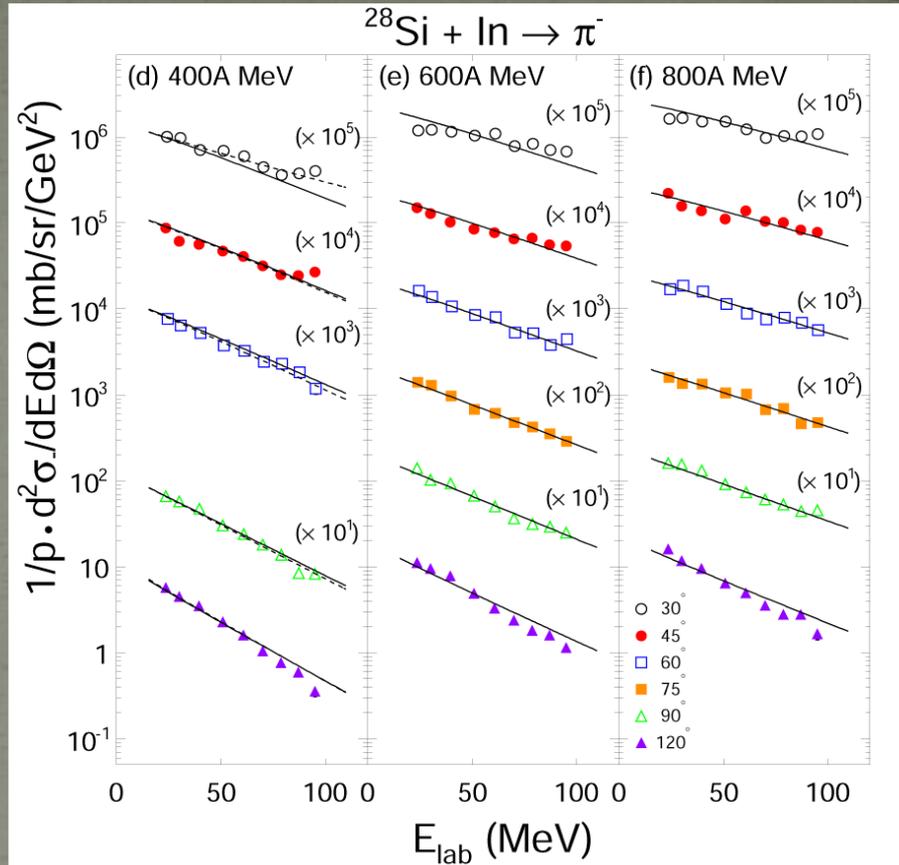
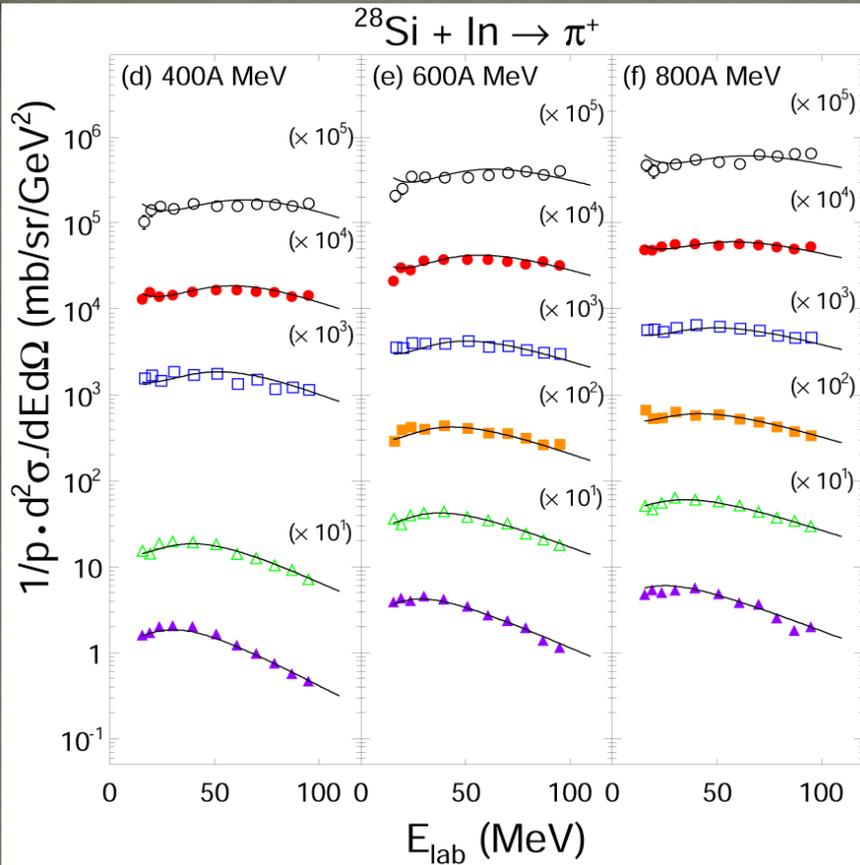
$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

·  $\mu^+$  : Energy ~ 4 MeV  
: Range ~ 1 mm

**Double pulse in one layer**

- $\sim 400 \text{ MeV/u}$   
Pion's are rare  
less than 1/100 of protons





$$f_-(E_{mov}) = N_- \exp(-E_{mov}/E_0),$$

$$f_+(E_{mov}) = N_+ P(E_{mov}) \exp(-E_{mov}/E_0),$$

$$E_{mov} = \gamma_{mov}(E_{lab} - \beta_{mov} p_{lab} \cos\theta_{lab}),$$

$$P(E_{mov}) = \Delta B_c / E_{mov} \ln\{1 + \exp[(E_{mov} - B_c)/\Delta B_c]\}.$$

$$1 + a_2 \cos^2 \theta_{mov} \quad p_{mov} \cos \theta_{mov} = \gamma_{mov}(p_{lab} \cos \theta_{lab} - \beta_{mov} E_{lab})$$

Using other functional form one couldn't fit data so well so far.....

# Fitting parameters

$E_{beam}$ (MeV)	$\beta_{mov}$	$E_0$ (MeV)	$N_-$	$N_+$	$B_c$	$\Delta B$	$a_2^*$
400A	0.19(1)	36.5(15)	13.8(8)	15.8(19)	28.4(19)	9.3(5)	–
	0.20(1)	37.0(12)	12.6(6)	14.6(13)	28.8(14)	9.5(4)	0.26(7)
600A	0.19(1)	44.3(16)	22.2(9)	23.0(20)	23.0(15)	8.5(5)	–
	0.19(1)	44.0(18)	22.6(11)	23.5(23)	23.0(16)	8.5(5)	-0.05(5)
800A	0.23(1)	51.8(23)	26.4(11)	25.7(23)	20.7(17)	9.1(6)	–
	0.22(1)	51.5(24)	27.2(13)	26.5(26)	20.8(17)	9.1(6)	-0.11(5)



$E_{beam}$ (MeV/nucleon)	$\sigma_{exp}(\pi^+)$	$\sigma_{exp}(\pi^-)$
400	0.33	0.63
600	0.87	1.37
800	1.41	2.10

Using moving source frame,  
it well overlaps.



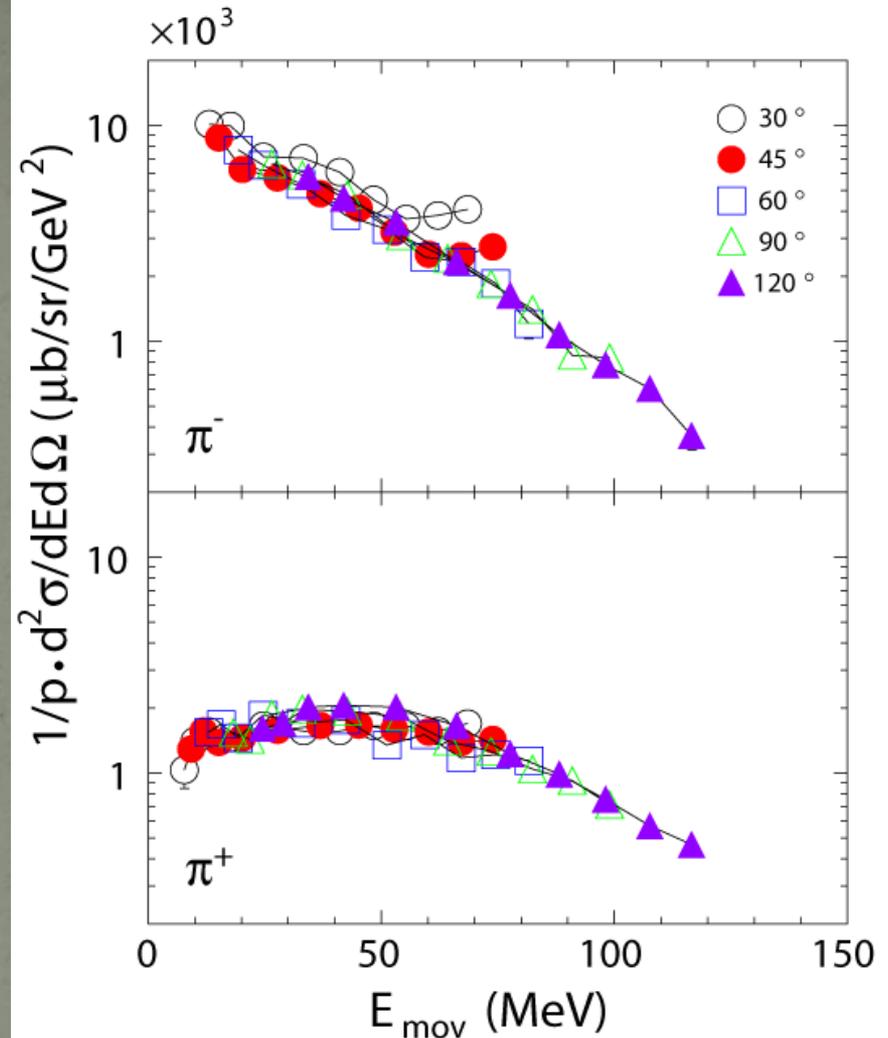
Isotropic emission  
from single moving source

Very slow!!!

**not mid-rapidity**

Similar phenomena have been observed by  
INDRA-ALADIN Collaboration; Eur. Phys. J. A 21, 293 (2004)

At 400MeV/nucleon



# Differential $\pi^-/\pi^+$ ratio

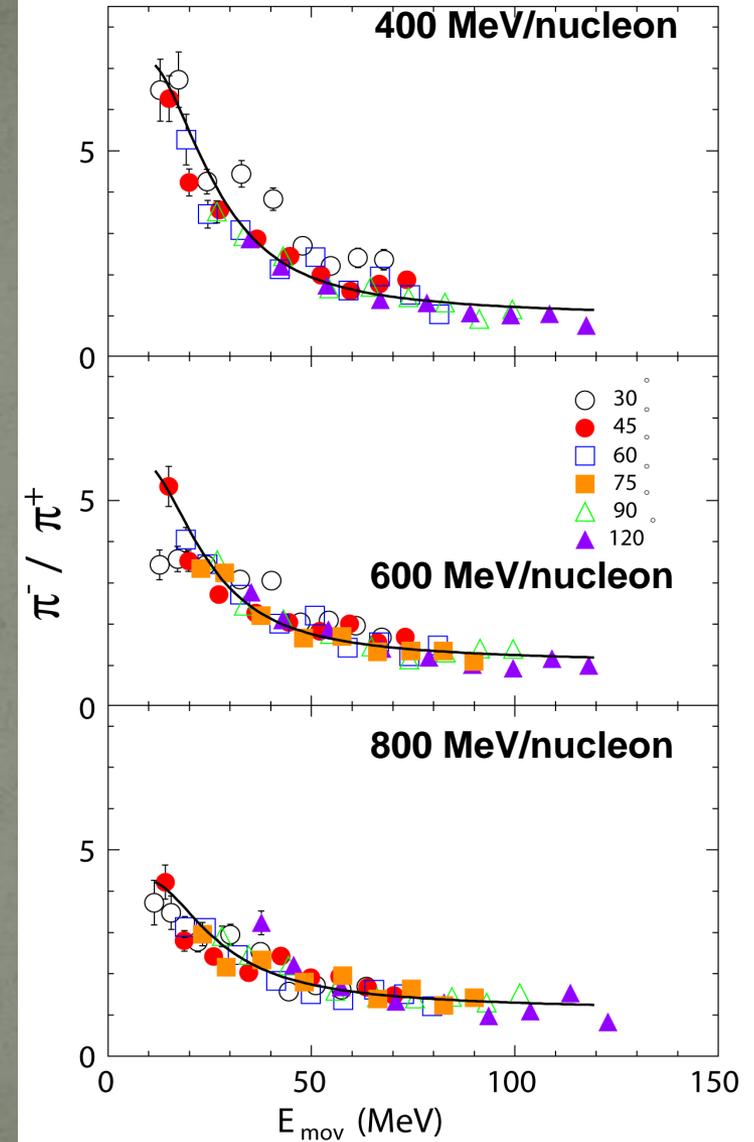


Weak angular dependence

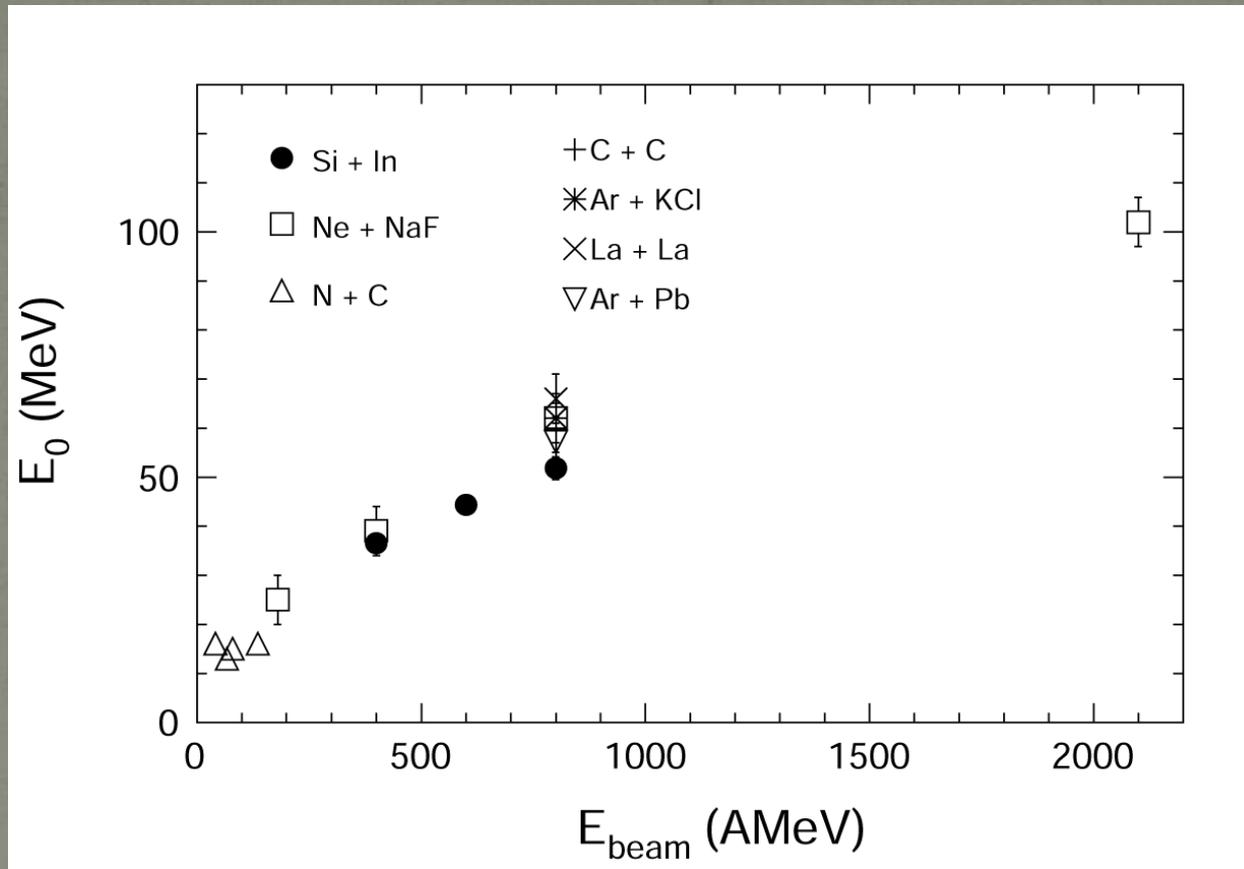
Clear energy dependence

**Simple Coulomb effect?**

Ratio alone can be fitted by functional form of Maheswari et al. (NP A628 (1998) 669), but It seems to be impossible to reproduce differential cross sections

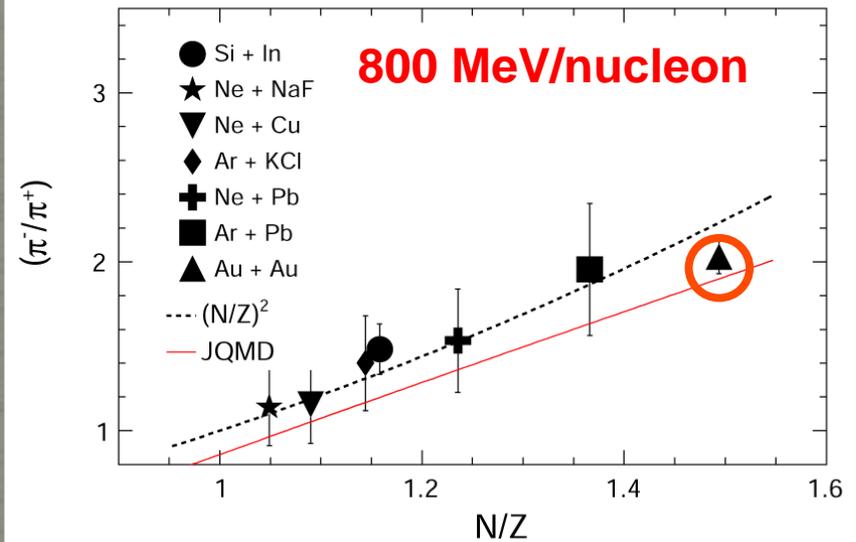
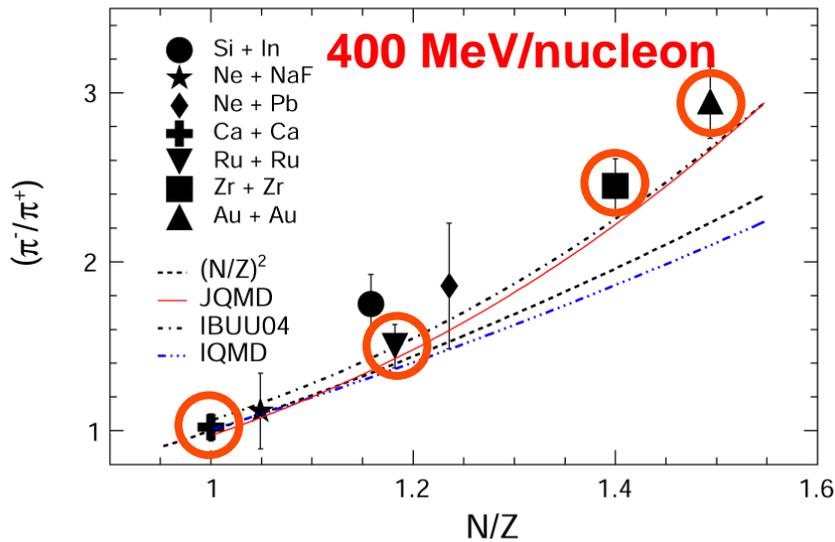


# Using fitted results



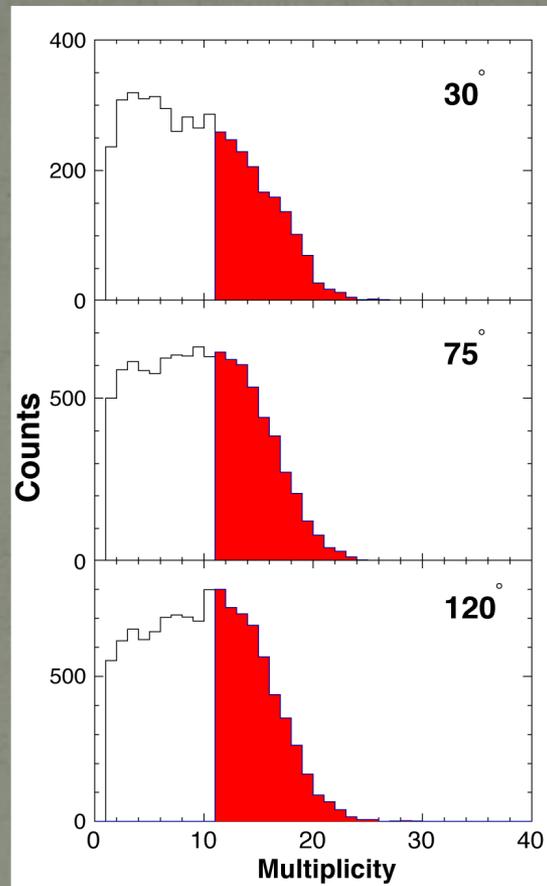
Slope parameters are consistent with old measurements

# $\pi^-/\pi^+$ total ratio vs $(N/Z)$ close to $(N/Z)^2$

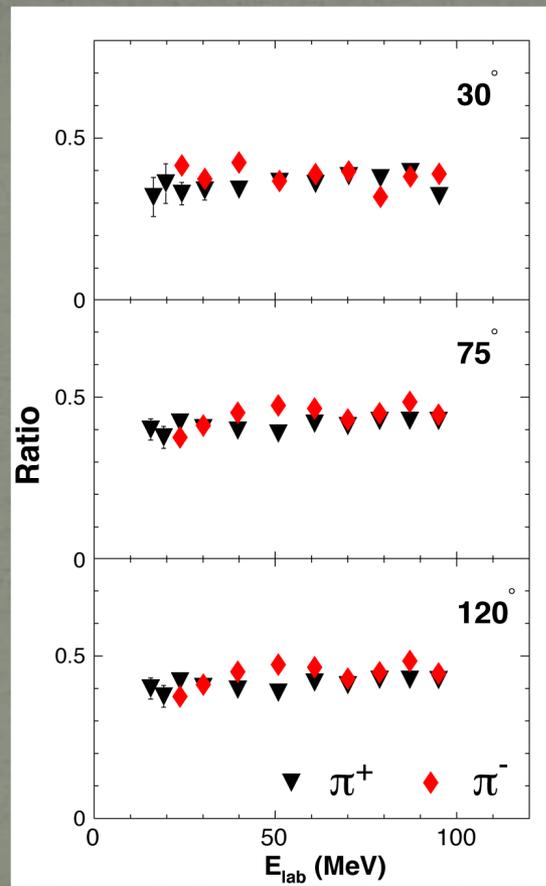


NB:  $N, Z$  are estimated for participant  
IBUU04, IQMD. **FOPI data** are for the central

# Example of Multiplicity dependence at 600 MeV/nucleon



$\pi^+$  associated multiplicity

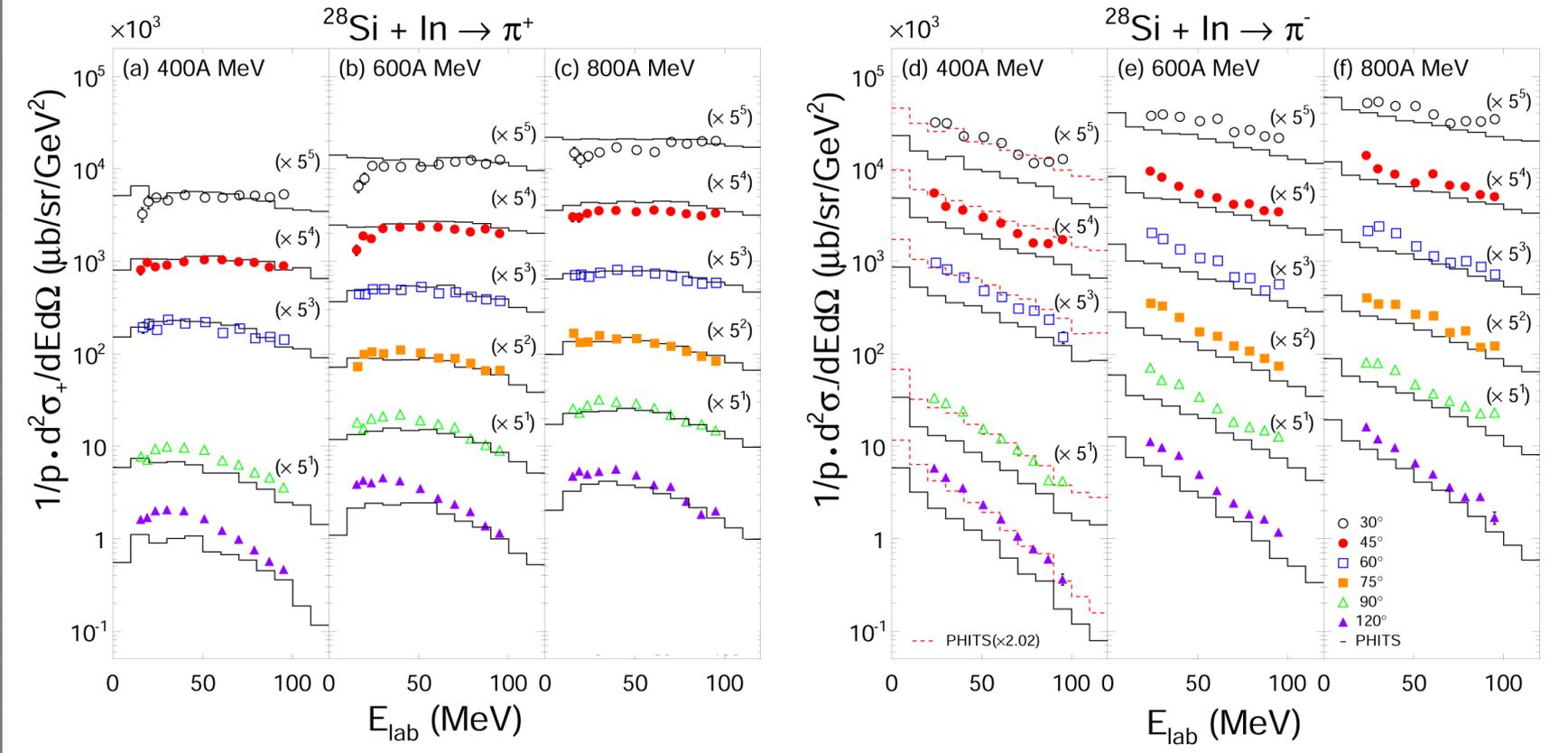


High multiplicity event/total event

Can we understand these features with a transport model?

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# Comparison with JQMD



**Normalization**  
**constant: 2.02, 1.68, and 1.43**

$E_{\text{beam}}$ (MeV/nucleon)	$\sigma_{\text{exp}}(\pi^+)$	$\sigma_{\text{exp}}(\pi^-)$	$\sigma_{\text{JQMD}}(\pi^+)$	$\sigma_{\text{JQMD}}(\pi^-)$
400	0.33	0.63	0.28	0.38
600	0.87	1.37	0.90	1.12
800	1.41	2.10	1.68	2.01

$\pm 7\%$

$\pm 10\%$

$E_{\text{beam}}$ (MeV/nucleon)	$\beta_{\text{mov}}(\text{c})$	$\beta_{\text{JQMD}}(\text{c})$	$\beta_{\text{CM}}(\text{c})$	$\beta_{\text{part}}(\text{c})$	$\beta_{\text{mid}}(\text{c})$
400	0.20(0.05)	0.31(0.02)	0.18	0.34	0.42
600	0.19(0.04)	0.34(0.04)	0.22	0.41	0.49
800	0.22(0.04)	0.35(0.06)	0.26	0.46	0.55

# Summary

- Measured doubly differential cross sections of  $\pi^+$  and  $\pi^-$  for the  $^{28}\text{Si} + \text{In}$  reactions at 400, 600 and 800 MeV/nucleons.
- They are emitted almost isotropically from the single moving source, whose velocity is quite slower than the mid rapidity.
- The differential pion ratios represented in such moving frames overlap each other at each incident energy.
- PHITS fails to reproduce the observed absolute cross section, the angular dependence of the cross sections and the charged pion ratio.

# Collaborators

M, Sako<sup>1;2</sup>,  
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